# The Importance of Being Earnest in Crowdsourcing Systems

Alberto Tarable<sup>1</sup>, Alessandro Nordio<sup>1</sup>, Emilio Leonardi<sup>1,2</sup>, Marco Aimone Marsan<sup>1,2,3</sup>

<sup>1</sup>CNR-IFIIT

<sup>2</sup>Politecnico di Torino

<sup>3</sup>IMDFA Networks Institute

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- integrate a large number of human and/or computer efforts

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- the correct task solution is obtained from answers through a decision rule

### **Assumptions**

• T binary tasks whose outcome is represented by i.i.d. uniform random variables (RV's)  $\tau_1, \tau_2, \ldots, \tau_T$  over  $\{\pm 1\}$ , i.e.,  $\mathbb{P}\{\tau_t = \pm 1\} = \frac{1}{2}$ ,  $t = 1, \ldots, T$ 

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- W workers, each one modeled as a binary symmetric channel (BSC); i.e., providing a wrong answer with probability  $p_{tw}$  and a correct answer with probability  $1 p_{tw}$

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Better performance can be achieved by designing smarter assignment schemes and decision rules!

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Understanding the potential impact of a-priori information about worker reliability is extremely important

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  - each worker belongs to one of K classes,  $C_1, C_2, \ldots, C_K$
  - each class is characterized, for each task, by an average error probability  $\pi_{tk}$ , known to the requester
- two extreme scenarios are possible:
  - Full Knowledge: the error probability of each worker in  $C_k$  is deterministically equal to  $\pi_{tk}$  for task t (zero variance case)
  - Hammer-Spammer (HS): perfectly reliable and completely unreliable users coexists within the same class (maximum variance case)

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  - no more than  $r_w$  tasks can be assigned to worker w
  - the total number of assignments cannot be larger than C

The task assignment we propose to approximate the optimum behavior is a simple greedy algorithm that starts from an empty assignment  $(\mathcal{G}^{(0)} = \emptyset)$ , and at every iteration i adds to  $\mathcal{G}^{(i-1)}$  the individual assignment  $(t, w)^{(i)}$ , so as to maximize an objective function P():

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$$(t, w)^{(i)} = \underset{(t, w) \in \mathcal{O} \setminus \mathcal{G}^{(i-1)}, (\mathcal{G}^{(i-1)} \cup \{(t, w)\}) \in \mathcal{F}}{\operatorname{arg max}} P(\mathcal{G}^{(i-1)} \cup \{(t, w)\})$$

The algorithm stops when no assignment can be further added to  $\mathcal{G}$ without violating the cost constraint C

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• 
$$P_1 = 1 - \frac{1}{T} \sum_t P_{e,t}$$

• 
$$P_2 = 1 - \max_t P_{e,t}$$

• 
$$P_3 = \sum_{t=1}^T I(\mathbf{a}_t; \tau_t)$$

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- Low Rank Approximation (LRA) rule [1]:

$$\hat{\tau}_t(\mathbf{a}_t) = \operatorname{sgn}\left(\sum_w a_{tw} v_w\right)$$

where  $v_w$  are the components of the leading right singular vector associated with the matrix of answers  $[a_{tw}]$ 

<sup>[1]</sup> D. R. Karger, S. Oh, D. Shah, "Budget-Optimal Task Allocation for Reliable Crowdsourcing Systems," *Operations Research*, vol. 62, no. 1, pp. 1–24, 2014.

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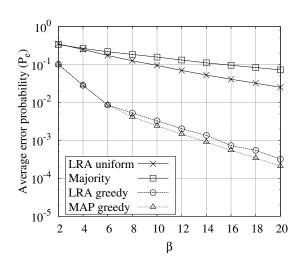
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### Results: a first scenario

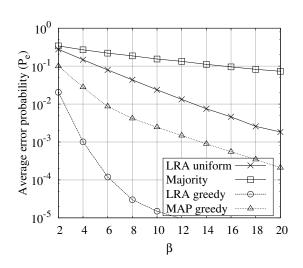
- Number of i.i.d tasks: T = 100
- 3 classes of workers:  $\pi_{t1} = 0.1, \pi_{t2} = 0.2, \pi_{t3} = 0.5$
- Number of workers per class:  $W_1 = 30$ ,  $W_2 = 120$ , and  $W_3 = 150$
- Maximum number of tasks per worker:  $r_w = 20$

## Full Knowledge



 $\beta$  is the average number workers per task

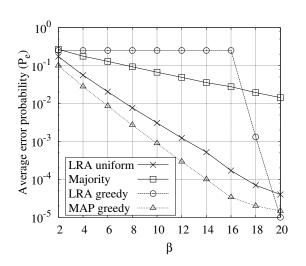
# Hammer-Spammer



### Results: a second scenario

- Two groups of 50 tasks each
- Error probabilities for the tasks in group 1 and 2 are given by  $\pi_{t_11}=0.1, \pi_{t_12}=0.25, \pi_{t_13}=0.5$   $\pi_{t_21}=0.5, \pi_{t_22}=0.25, \pi_{t_23}=0.1$
- Number of workers per class:  $W_1 = 40$ ,  $W_2 = 120$ , and  $W_3 = 40$
- Maximum number of tasks per worker:  $r_w = 20$

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- ullet even largely inaccurate estimates of workers' reputation during task assignment o large improvements of system performance
- a simple optimal task-independent MAP decision rule is proposed for the case of full knowledge of workers' reputation
- when workers' reputation estimates are significantly inaccurate, the best performance can be obtained by combining our proposed task assignment algorithm with advanced decision rules such as LRA

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