

# Thesis - Report Feb 10 - Heuristic Betweenness Centrality for Weighted Graph

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# 1 Introduction

## 1.1 Notation

**BBC**: the score obtained by Brandes Betweenness Centrality

**BBCT**: the score obtained by Brandes BC with the inclusion of targets

**HBCU**: the heuristic way to obtain BC score, for unweighted graph

**HBCW**: the heuristic way to obtain BC score, for weighted graph

## 1.2 Dataset

There are 5 datasets in total:

- Unweighted graphs
  - *simple*: this is the graph getting from paper [1]
  - *ninux\_unweighted\_connected*: all the vertices and edges are the same as *ninux\_30\_1*, but the costs for all edges are 1. It's
- Weighted graphs
  - *ninux\_30\_1*
  - *olsr-netjson*
  - *jsoninfo\_topo*

## 1.3 Comparison between BBC, BBCT, HBCU

We have  $BBC \sim HBCU$ , there are constant difference between the scores obtained by these 2 methods.

And we have  $BBCT = HBCU$ . See 1

## 1.4 Purpose

This report will

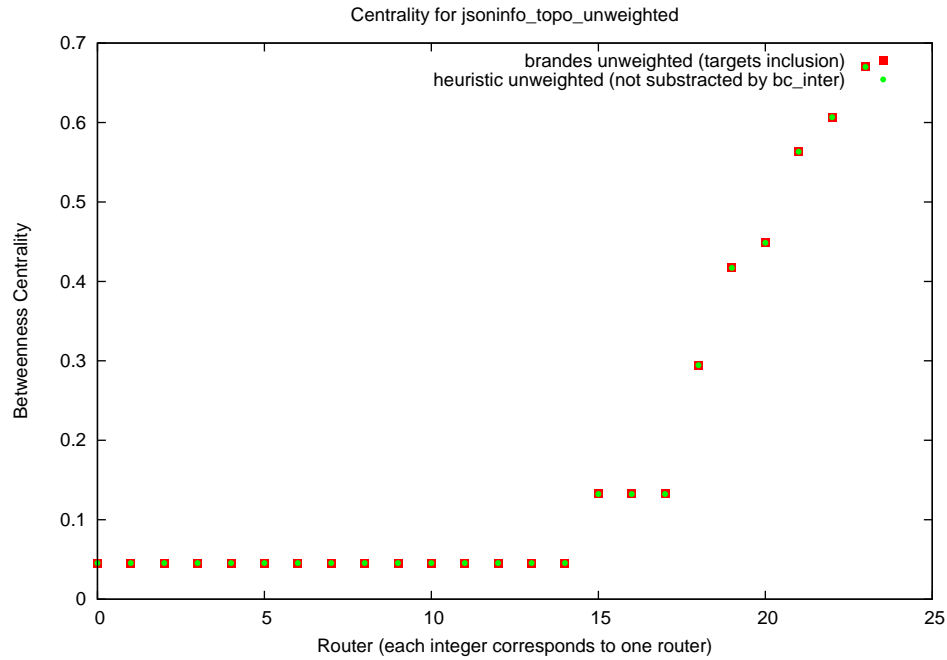
- Show how HBCW is obtained
- Comparing HBCU and HBCW

# 2 HBC for weighted graph

## 2.1 Method

When calculating the BC for each bi-connected component, *weight\_map* is included. As a result, HBCW will take into account the weight of each edge when calculating the number of shortest paths  $\sigma$ . The  $\sigma$  will affect the final BC score.

Figure 1: BBCT & HBCU for jsoninfo\_topo. Their results are the same



### 3 Result

For **unweighted graph**,  $BBCT = HBCW$ .

For **weighted graph**,  $BBCT = HBCW$  with these dataset:

- *ninux\_30\_1*. See 2
- *olsr-netjson*

And  $BBCT \neq HBCW$  in the dataset *jsoninfo\_topo*. See 3. Compare to the result obtained by HBCU in 1

Figure 2: BBCT & HBCW for ninux\_30\_1

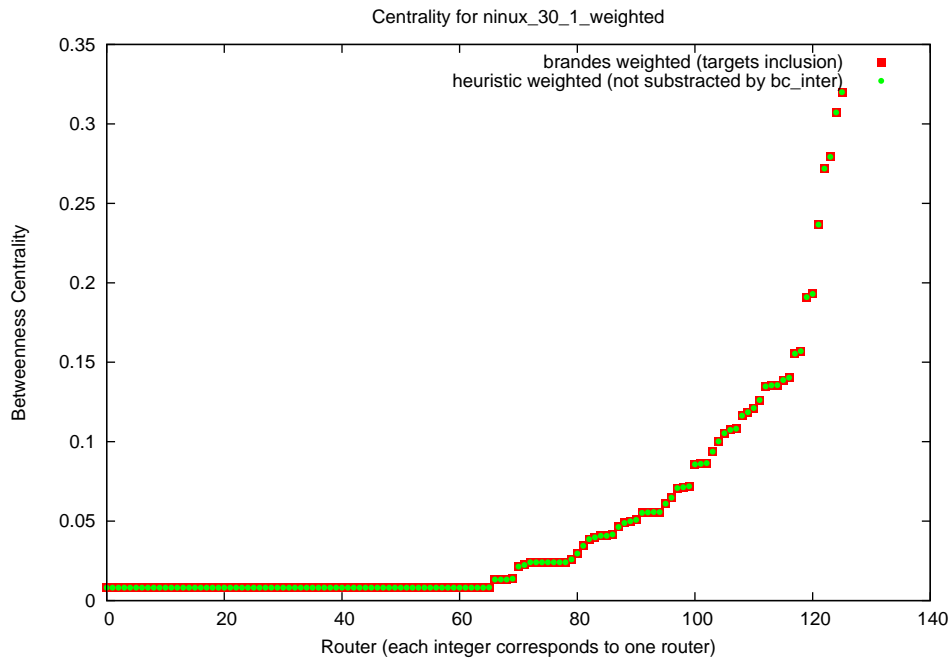
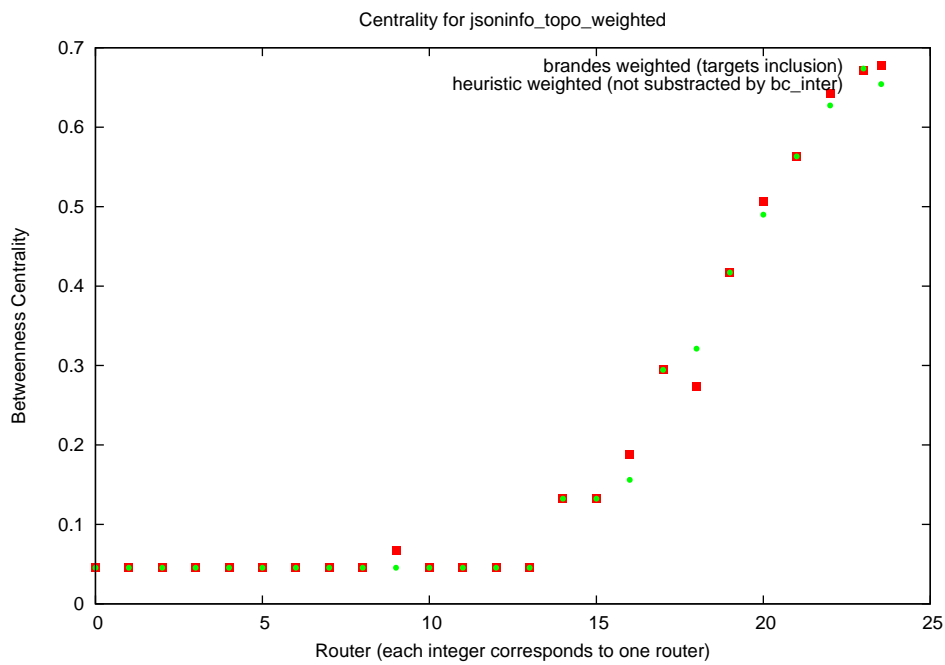


Figure 3: BBCT & HBCW for jsoninfo\_topo. Their results are different



## References

- [1] Rami Puzis, Polina Zilberman, Yuval Elovici, Shlomi Dolev, and Ulrik Brandes. Heuristics for speeding up betweenness centrality computation. In *2012 International Conference on Privacy, Security, Risk and Trust, PASSAT 2012, and 2012 International Conference on Social Computing, SocialCom 2012, Amsterdam, Netherlands, September 3-5, 2012*, pages 302–311, 2012.